

Billiards notation

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γ	a closed geodesic on the double of a triangle, $\mathcal{D}(T)$
$\hat{\gamma}$	a periodic billiard path in a triangle
Δ	the parameter space of marked triangles
$\mathcal{D}, \mathcal{D}(T)$	double of a triangle T across its edges (an Euclidean cone surface)
F	a defining function for an edge of $O(W)$ ($F = \text{Im}(\pm P\bar{Q})$)
$H, H(W)$	the <i>hexpath</i> (the path in the hexagonal grid corresponding to the combinatorial type W)
$\text{MT}, \text{MT}(T)$	the minimal translation surface corresponding to a triangle T
$O, O(W)$	an <i>orbit tile</i> corresponding to the word W (ie. the collection of triangles with billiard paths of combinatorial type W)
P	part of defining function for and edge of $O(W)$ (a map $\Delta \rightarrow \mathbb{C}$)
Q	part of defining function for and edge of $O(W)$ (a map $\Delta \rightarrow \mathbb{C}$)
$\hat{Q}, \hat{Q}(W)$	the <i>square path</i> , which is related to $H(W)$
T	a triangle

$U, U(W, T)$	<i>unfolding</i> of triangle T with respect to combinatorial type W
$UAC, UAC(X)$	the <i>universal abelian cover</i> of the space X (X defaults to the 3-punctured sphere)
V_n	the Veech triangle with angles $(\pi/2n, \pi/2n, (\pi - 1)/n)$
W	a <i>combinatorial type</i> (ie. an infinite periodic word in the letters $\{1, 2, 3\}$, representing edges hit by a potential periodic billiard path)